

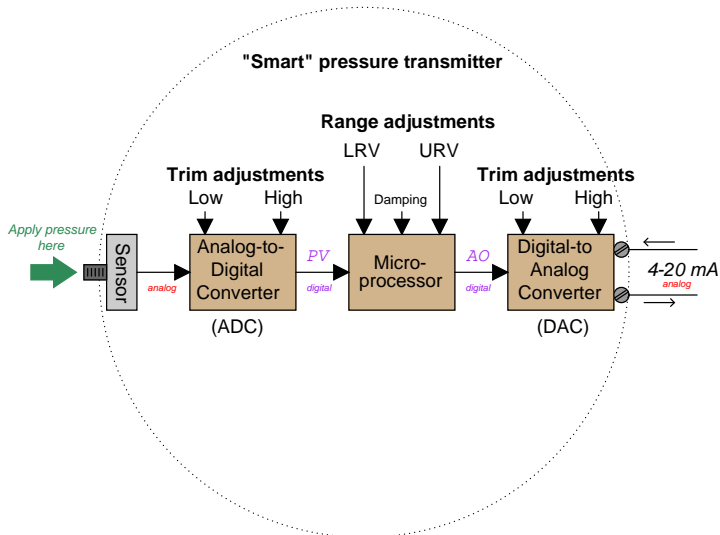
# Technical Means of Automation

## Sensor Characteristics

Institute of Information Engineering, Automation and Mathematics

September 27, 2016

# Sensor - Transmitter



# Sensor Characteristics

## Static characteristics:

- Range
- Sensitivity
- Offset and drift
- Precision
- Accuracy
- Resolution (discrimination)
- Linearity
- Hysteresis
- Stability
- Errors

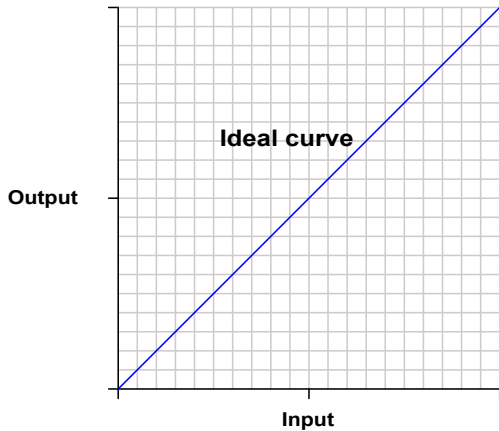
## Dynamic characteristics:

- Zero order system
- First order system
- Second order system
- Sampling rate

# Static Characteristics

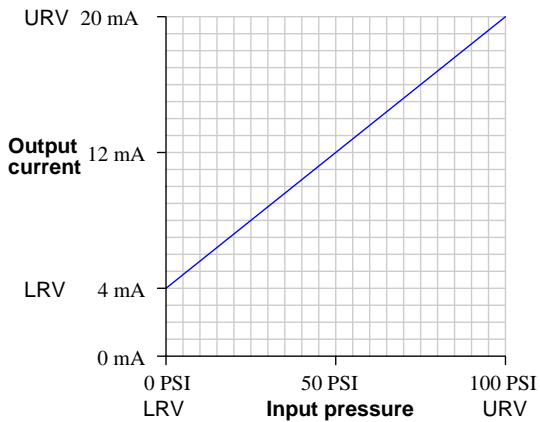
# Sensor Characteristics

Ideal (perfect) sensor



# Sensor Characteristics

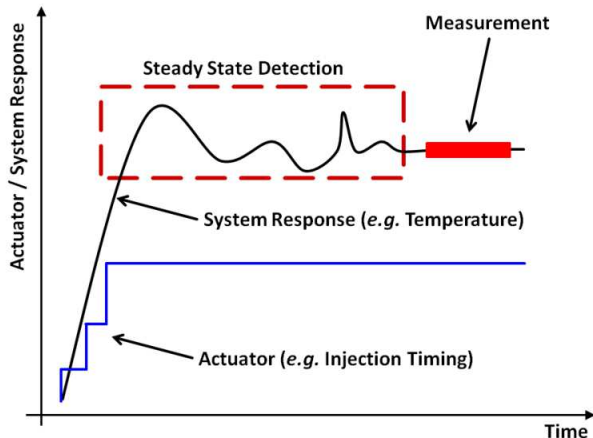
Ideal pressure sensor



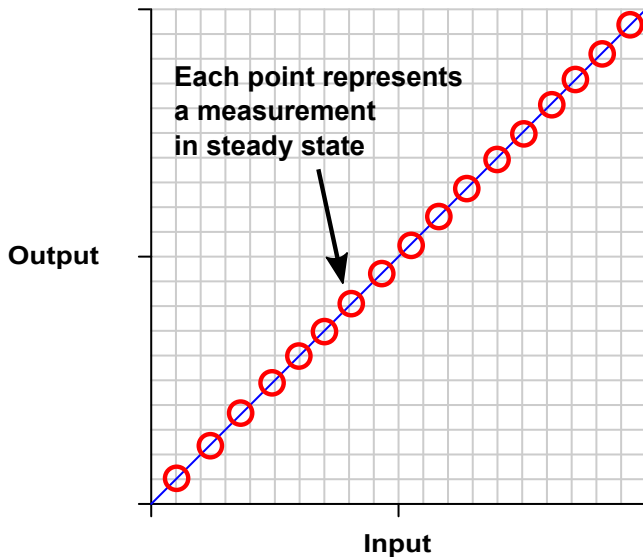
# Static Characteristics

The properties of the system after all transient effects have settled to their final or steady state.

## Steady state



# Static Characteristics





# How to Obtain Static Characteristics?

Calibration of sensor:

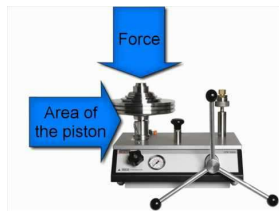
- 1 force system's quantity to LRV steady state (reference)
- 2 perform sensor's output and reference measurement (evaluate 5)
- 3 force system's quantity a step ahead of last reference measurement
- 4 let system to reach steady state (go to 2)
- 5 if measurement reaches URV: continue to 6; else: go back to 3
- 6 record data and perform 1-5 for opposite direction URV to LRV
- 7 now you have all the data to plot static characteristic of sensor

# What is the Reference Measurement?

Reference measurement is a reliable method to determine an actual value of physical quantity.

Some examples of reference measurements:

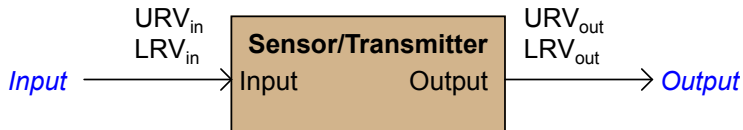
- range/distance - rulers, meter sticks
- temperature - boiling water ( $100\text{ }^{\circ}\text{C}$ ) and ice bath ( $0.01\text{ }^{\circ}\text{C}$ ) at sea level
- pressure - Dead Weight Tester
- acceleration - gravity is a constant ( $1\text{G}$ ) on the surface of the earth



## Range

- Input range (e.g. 20 – 150 °C, 250 – 800 PSI, ...)
  - represents a maximum and minimum value of the physical variable that can be measured
  - determines the applicability of sensor for **physical conditions**
- Output range (e.g. 4 – 20 mA, 0 – 10 V)
  - represents a maximum and minimum value of signal produced by sensor/transmitter
  - corresponds to measured quantity
  - determines the applicability of sensor for **data acquisition equipment**

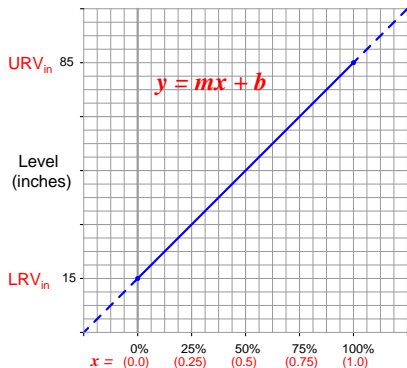
## Static Characteristics - Range



$$\frac{Input - LRV_{in}}{URV_{in} - LRV_{in}} = \text{Per unit of span (from 0 to 1 inclusive)} = \frac{Output - LRV_{out}}{URV_{out} - LRV_{out}}$$

# Static Characteristics - Range

**Input range = 15 to 85 inches liquid level**



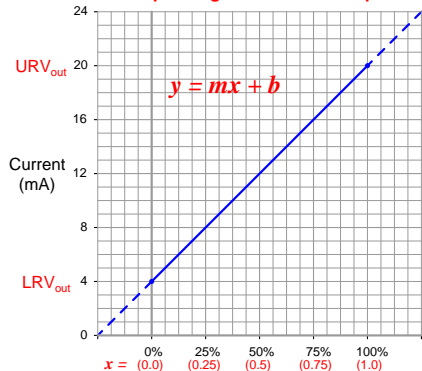
Signal (x) expressed as a per unit ratio

$$y = (85 - 15)x + 15$$

$$y = 70x + 15$$

$$\text{Input} = (\text{URV}_{in} - \text{LRV}_{in})(\text{per unit}) + \text{LRV}_{in}$$

**Output range = 4 to 20 milliamps**



Signal (x) expressed as a per unit ratio

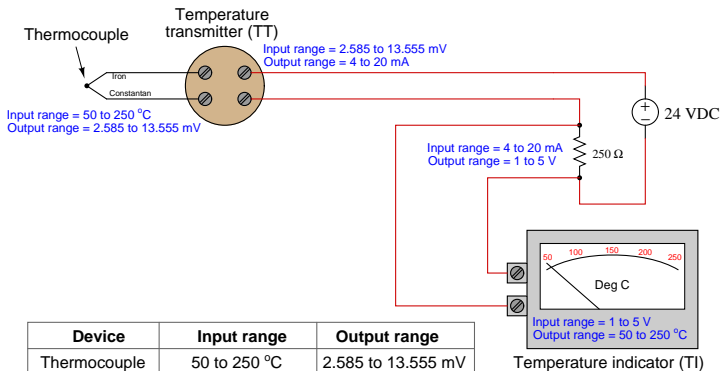
$$y = (20 - 4)x + 4$$

$$y = 16x + 4$$

$$\text{Output} = (\text{URV}_{out} - \text{LRV}_{out})(\text{per unit}) + \text{LRV}_{out}$$

# Static Characteristics - Range

Actually, there are more ranges in sensing system.



Device	Input range	Output range
Thermocouple	50 to 250 °C	2.585 to 13.555 mV
Transmitter	2.585 to 13.555 mV	4 to 20 mA
Resistor	4 to 20 mA	1 to 5 V
Indicator	1 to 5 V	50 to 250 °C

## Sensitivity

Determines how large response of sensor is produced by a normalized change of input (usually one-step increment).

- **gain** of sensor's transfer function
- represented by a **slope** of calibration curve  $y(x) = f(x) = \mathbf{ax} + b$

Possible scenarios (positive gain):

gain  $\approx 1$  - medium sensitivity, 1-to-1 proportional, smallest information loss

gain  $> 0$  - good sensitivity, possible information loss

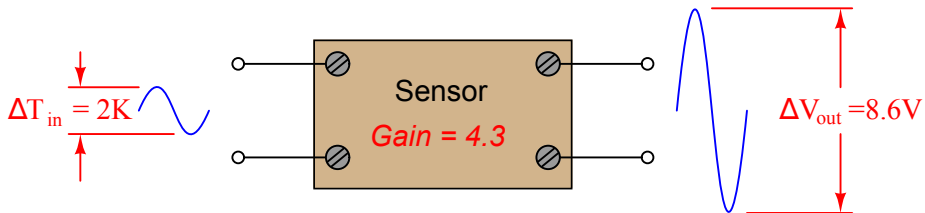
$1 > \text{gain} > 0$  - poor sensitivity, possible information loss

gain  $> 1$  - high sensitivity, possible information loss

gain  $\rightarrow \text{inf}$  - extreme sensitivity, high information loss

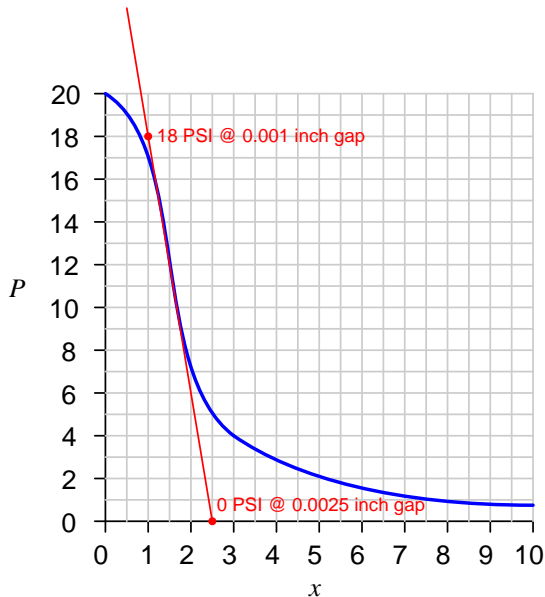
gain  $\rightarrow 0$  - no sensitivity, high information loss

## Static Characteristics - Sensitivity





## Static Characteristics - Sensitivity



# Static Characteristics - Offset (zero shift) and drift

## Offset

Determines the value of shift of static characteristics in y-axis from the zero reference.

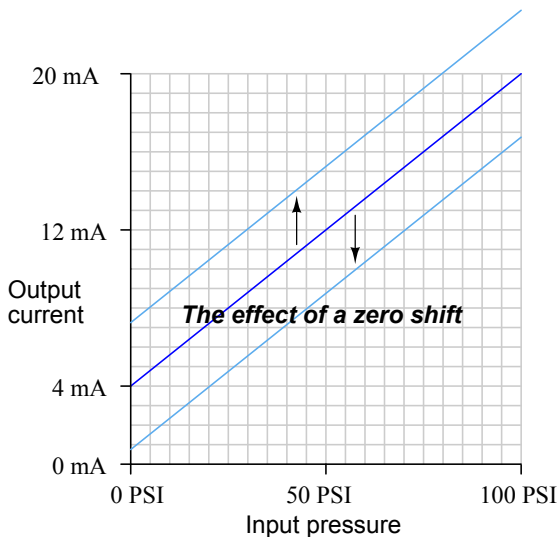
- represented by a **intercept** of calibration curve  $y(x) = f(x) = ax + \mathbf{b}$
- simple correction - shift the curve back to origin

## Drift

Determines how the offset is changing in time.

- long-time effect – wear of sensor
- short-time effect – variable physical interference

## Static Characteristics - Offset (zero shift) and drift

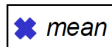
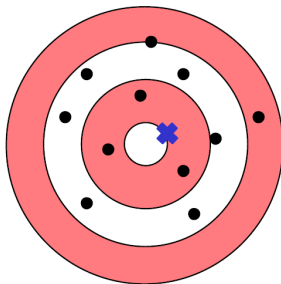
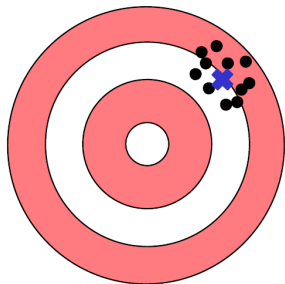


## Precision vs Accuracy



## Static Characteristics - Precision vs Accuracy

Which one is more accurate?



## Precision vs. Accuracy

Precision:

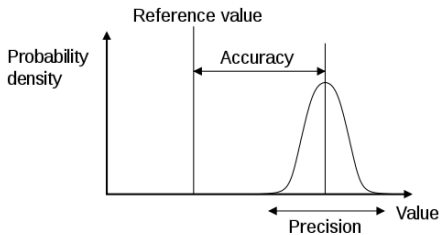
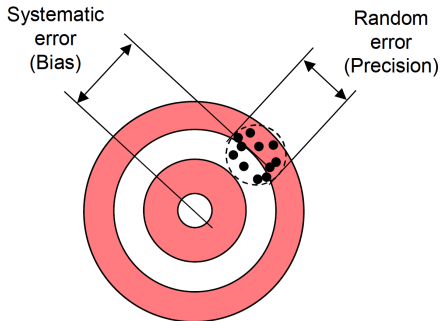
- degree of **reproducibility** of measurement
- ideal sensor provides exactly same values over numerous measurements
- measured value is not necessarily the true value of quantity

Accuracy:

- a maximum **difference between true and measured value** of quantity
- is related to the **bias** of a set of measurements
- inaccuracy – error
- various representations:
  - Absolute error = Result – True value
  - Relative error =  $\frac{\text{Absolute error}}{\text{True value}}$

# Static Characteristics - Precision vs. Accuracy

## Precision vs. Accuracy



## Resolution (Discrimination)

Resolution is the minimal change of the input necessary to produce a detectable change at the output.

- increment from zero – **threshold**
- domain of analog world
- perfect analog sensor – infinite resolution

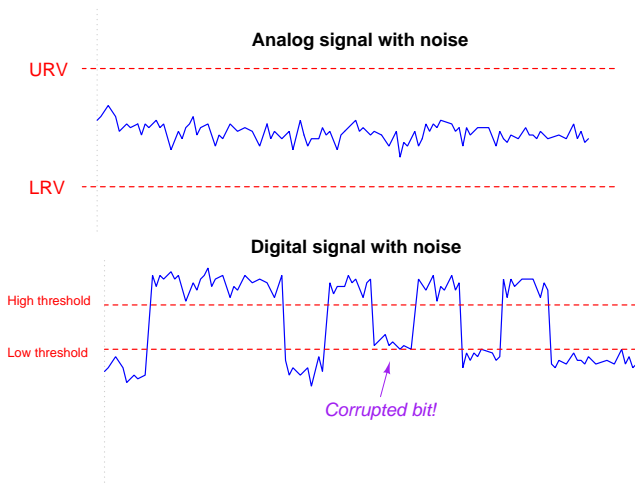
What can contribute to loss of resolution?

- electrical noise ( $\text{SNR} \gg 1$ )
- analog-to-digital quantization



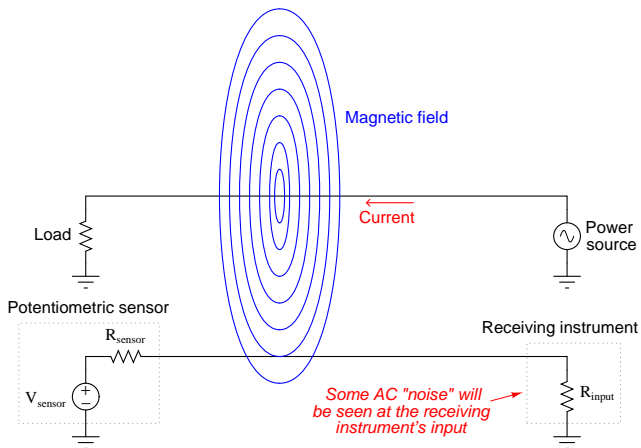
# Static Characteristics - Impact of Noise on Resolution

## Noise (Analog vs Digital)



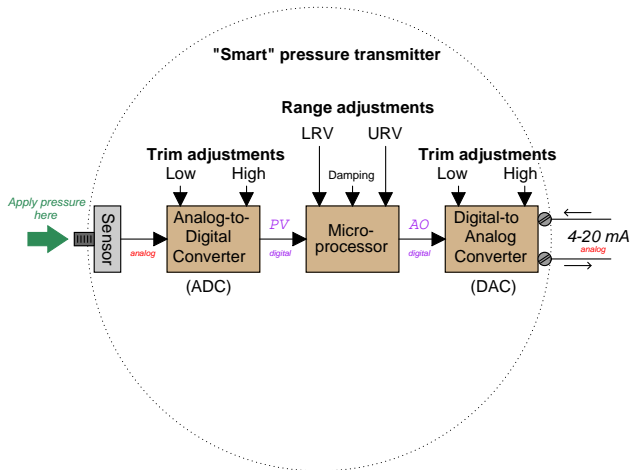
# Static Characteristics - Impact of Noise on Resolution

## Noise (Source)



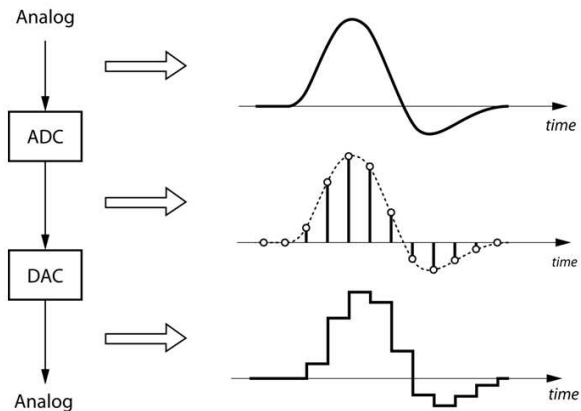
# Static Characteristics - ADC Impact on Resolution

## Analog to Digital Conversion (Quantization)



# Static Characteristics - ADC Impact on Resolution

## Analog to Digital Conversion (Quantization)

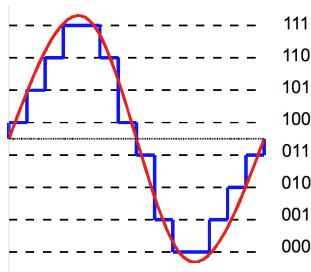
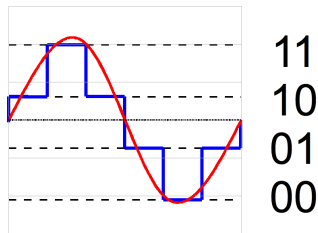


# Static Characteristics - ADC Impact on Resolution

## Analog to Digital Quantization

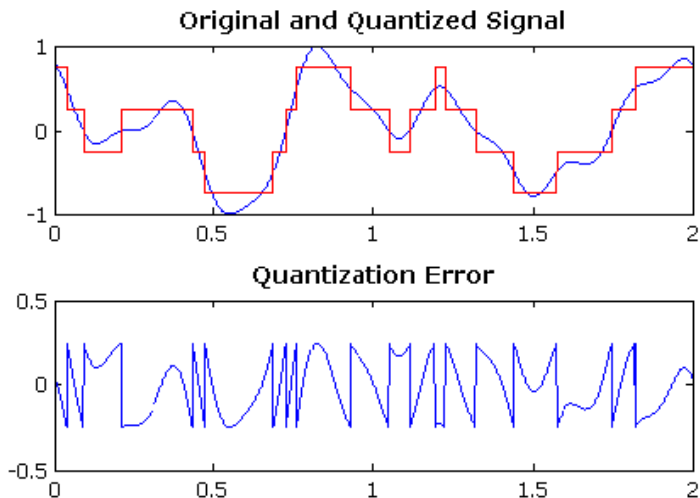
Quantization is mapping of large data sets into a smaller set.

- analog to digital converters (ADC)
- actual measurement is transferred into binary representation
- loss of information – **quantization error**



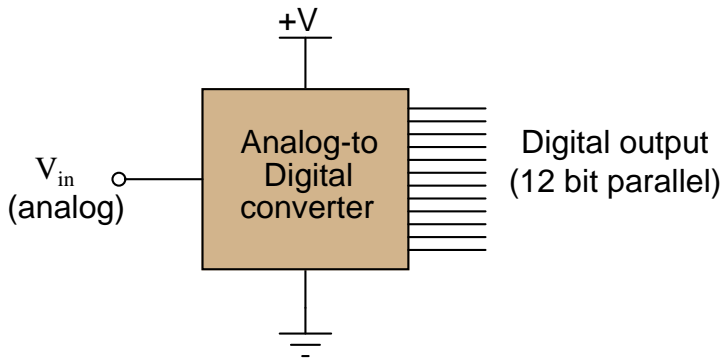
## Static Characteristics - ADC Impact on Resolution

### Quantization Error

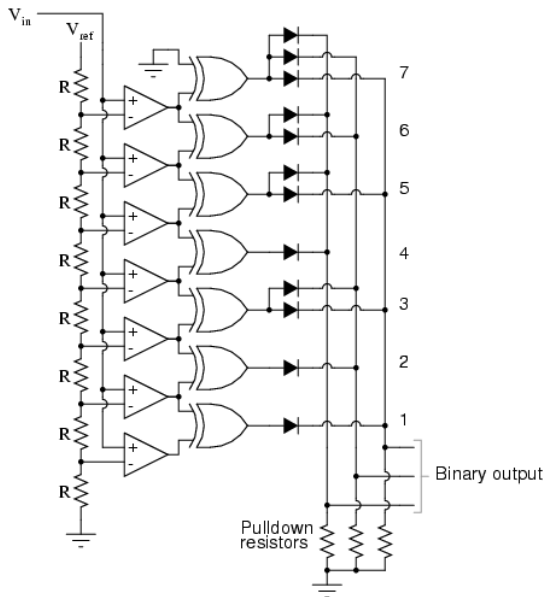


## Static Characteristics - ADC Impact on Resolution

### Analog to Digital Converters



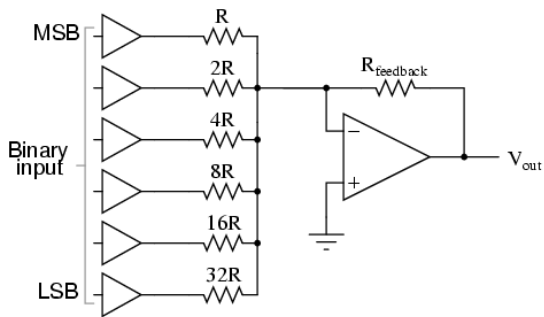
# Simple ADC Schematics





# Simple DAC Schematics

*6-bit binary-weighted DAC*



# Static Characteristics - ADC Impact on Resolution

## Analog to Digital Converters

Resolution of ADC/DAC:

$$\text{Analog resolution} = \frac{\text{Analog range}}{2^n - 1}$$

Numerical representation of input:

$$\frac{V_{in}}{V_{range}} = \frac{\text{Counts}}{2^n - 1}$$

$V_{in}$	Counts (dec,12-bit)
0 V	0
2.46 mV	1
3.85 V	1576
4.59 V	1879
6.11 V	2502
9.998 V	4094
10 V	4095

## Static Characteristics - ADC Impact on Resolution

Decimal range vs. number of bits

bits	range unsigned	Range signed
8	0 – 255	-127 – 127
10	0 – 1023	-511 – 511
12	0 – 4095	-2 047 – 2 047
14	0 – 16 383	-8 191 – 8 191
16	0 – 65 535	-32 768 – 32 768
20	0 – 10 048 575	-524 287 – 524 287
24	0 – 16 777 216	-8 388 607 – 8 388 607

# Static Characteristics - ADC Impact on Resolution

**Task 1** – calculate the analog resolution of ADC (in voltage and Kelvin) for following case:

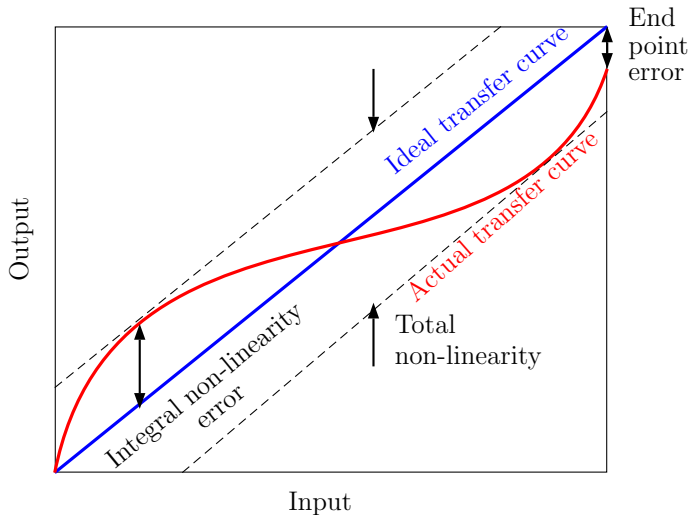
- range of quantity: 0–150K (temperature)
- range of input: 0–10V
- 8-bit ADC

**Task 2** – calculate the measured pressure if:

- range of quantity: 10–400 kPa
- range of input: -10–10V
- 10-bit ADC
- ADC returns a decimal number of 524

# Static Characteristics - Linearity

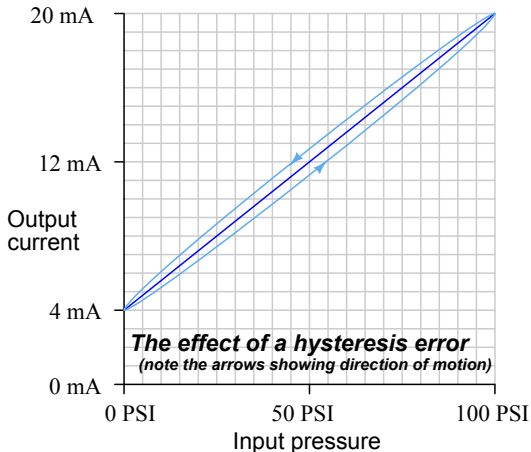
## Linearity



# Static Characteristics - Hysteresis

## Hysteresis

The difference between two output values that correspond to the same input depending on the trajectory followed by the sensor.



## Stability

The ability of a sensor to retain its performance characteristics for a relatively long period of time. Unless otherwise stated, stability is the ability of a sensor to reproduce output readings obtained during its original calibration, at room conditions, for a specified period of time. It is then typically expressed as being *within X percent* of full scale output or *measured units* for a period of *Y months*.

- freedom from undesirable deviation
- a measure of controllability of process
- related to sensitivity, offset, drift, accuracy, precision, resolution and linearity
- main cause – aging of sensor

## Errors

Systematic errors – result from a variety of (often **human**) factors

- interfering or modifying variables
- measurement process changes the value of process quantity
- improper range selection (non-monotonic characteristics)
- human observers (parallax error)

Random errors – **this is not our fault!**

- a signal that carries no information (noise)
  - caused by inability to reproduce the measurement
  - environmental noise
  - transmission noise
- true random errors
  - Gaussian distribution
  - white noise

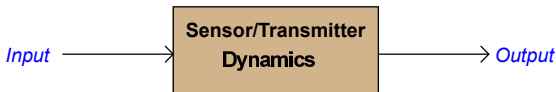


# Dynamic Characteristics

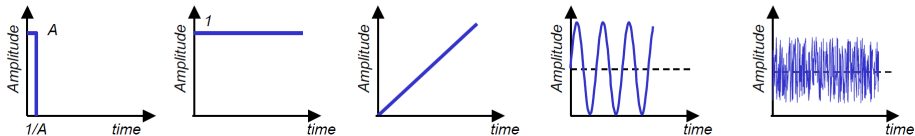
# Dynamic Characteristics

The sensor response to a variable input is different from that exhibited when the input signals are constant (static characteristics).

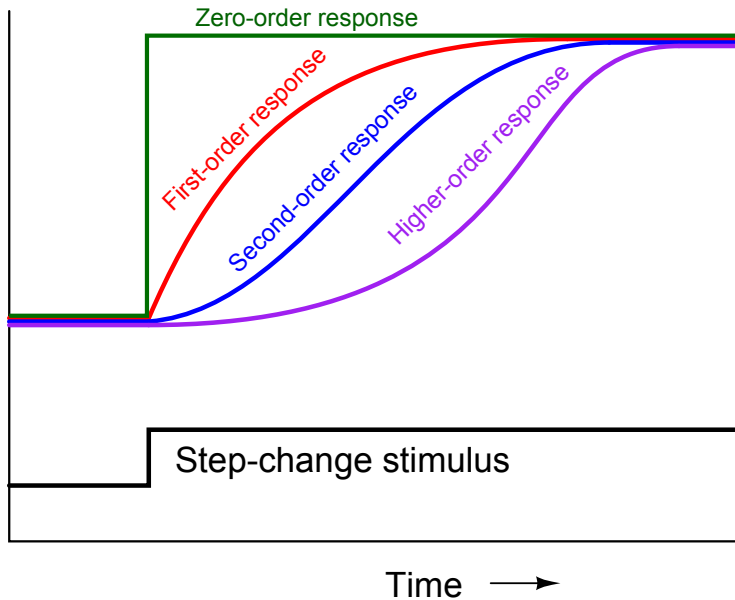
How the sensor acts as the dynamical input-output system?



Dynamic characteristics are determined by analyzing the response of the sensor to a family of variable input waveforms:



# Dynamic Characteristics - Step Response



# Dynamic Characteristics – Zero-Order Sensor

Input and output of sensor are related by a algebraic equation:

$$y(t) = k \cdot x(t) \Rightarrow \frac{Y(s)}{X(s)} = k$$

Zero-order sensor – perfect sensor:

- no dynamics
- acts only as amplifier
- no accumulation of energy or mass

Examples:

- electric circuit switches
- potentiometers

# Dynamic Characteristics – First-Order Sensor

Input and output of sensor are related by an equation:

$$a_1 \frac{dy(t)}{dt} + a_0 y(t) = x(t) \Rightarrow \frac{Y(s)}{X(s)} = \frac{1}{a_1 s + a_0} = \frac{k}{Ts + 1}$$

First-order sensor:

- step response:  $y(t) = \Delta x(t) \cdot k \left(1 - e^{-\frac{t}{T}}\right)$
- characterized by time constant and gain
- accumulation of energy or mass

Examples:

- thermistor
- thermocouple

# Dynamic Characteristics – Second-Order Sensor

Input and output of sensor are related by an equation:

$$a_2 \frac{d^2 y(t)}{dt^2} + a_1 \frac{dy(t)}{dt} + a_0 y(t) = x(t) \Rightarrow \frac{Y(s)}{X(s)} = \frac{1}{a_2 s^2 + a_1 s + a_0}$$

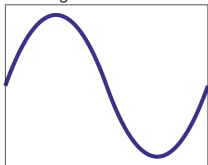
Second-order sensor:

- characterized by:
  - time to peak
  - peak overshoot
  - settling time and value
- response types:
  - underdamped ( $\xi < 1$ )
  - critically damped ( $\xi = 1$ )
  - overdamped ( $\xi > 1$ )
- accumulation of energy or mass in two elemental subsystems in series

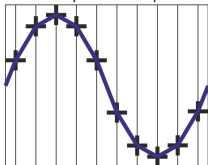
# Dynamic Characteristics – Sampling

How often we perform the measurements of the physical quantity.

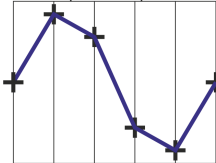
Original Waveform



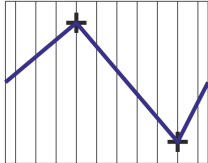
Sampled at 10 points



Sampled at 6 points



Sampled at 2 points



Nyquist Sampling Theorem:  
*“The absolute minimum sample rate necessary to capture an analog waveform is twice the waveform’s fundamental frequency.”*

